

# 中国科学院国家天文台

National Astronomical Observatories, CAS



the SILK ROAD PROJECT at NAOC

# 丝绸之路 计划

RECRUITMENT  
PROGRAM OF GLOBAL EXPERTS



## Direct N-Body Simulations

Deutsche  
Forschungsgemeinschaft  
SFB881 DFG

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\*Special State Foreign Expert in Thousand People's Plan in China

**NVIDIA**  
World Leader in Visual Computing Technologies

**EGO** EUROPEAN  
GRAVITATIONAL  
OBSERVATORY

Volkswagen **Stiftung**



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Rainer Spurzem

CAS Visiting Professor, Senior  
International Scientists  
Professor at Heidelberg University (on  
partial leave)

Picture: Luca Naso



Gareth Kennedy

Postdoc (CAS Fellow)



Xiaoying Pang

Postdoc at NAOC



Siyi Huang

Graduate student



Shuo Li

Postdoc (NAOC)



Shiyan Zhong

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Lei Liu

Graduate student at:  
(1) Astronomisches Rechen-Institut,  
Zentrum fuer Astronomie, Heidelberg  
University  
and (2) National Astronomical  
Observatories, CAS)



Peter Berczik

Senior Silk Road Project Postdoc



Yohai Meiron

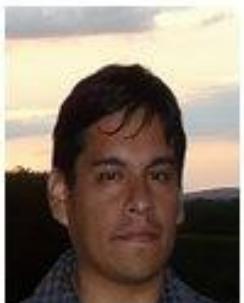
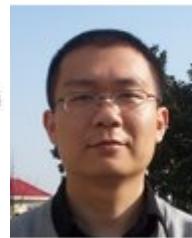
Postdoc (KIAA-PKU)



**POSTER!**

Long Wang

Ph. D. Student (Peking  
University)



Jose Fiestas

Postdoc at NAOC



Maxwell Tsai (aka. Xu CAI)

Ph. D. Student (NAOC)



**RECRUITMENT**  
PROGRAM OF GLOBAL EXPERTS



Thijs Kouwenhoven

Balren research professor at KIAA



# 北京大学

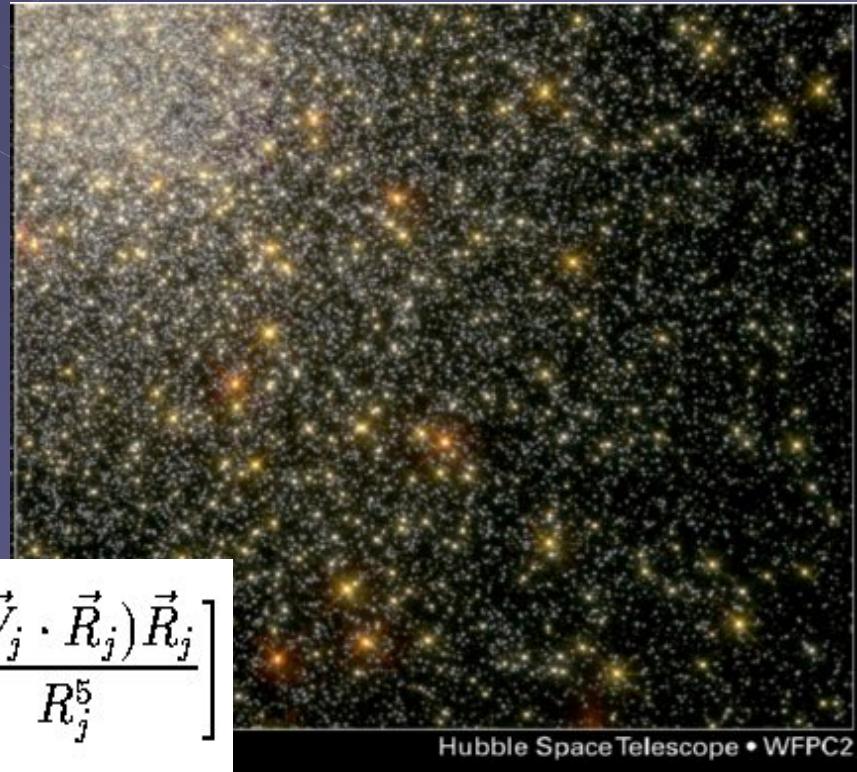
PEKING UNIVERSITY

Aspen Jan. 2015

# Star Cluster Simulations – Key Issues

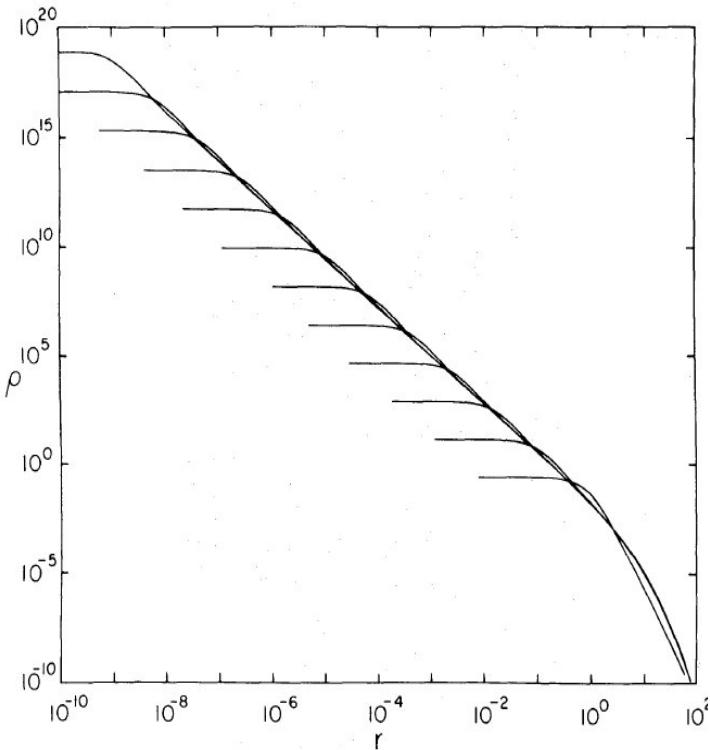
- Theoretical Models / Large N-Body Models
- Black Holes and Tidal Disruption/Star Accretion
- Accelerated Computing (GPU)

$$\vec{a}_0 = \sum_j G m_j \frac{\vec{R}_j}{R_j^3} ; \quad \vec{a}_0 = \sum_j G m_j \left[ \frac{\vec{V}_j}{R_j^3} - \frac{3(\vec{V}_j \cdot \vec{R}_j)\vec{R}_j}{R_j^5} \right]$$

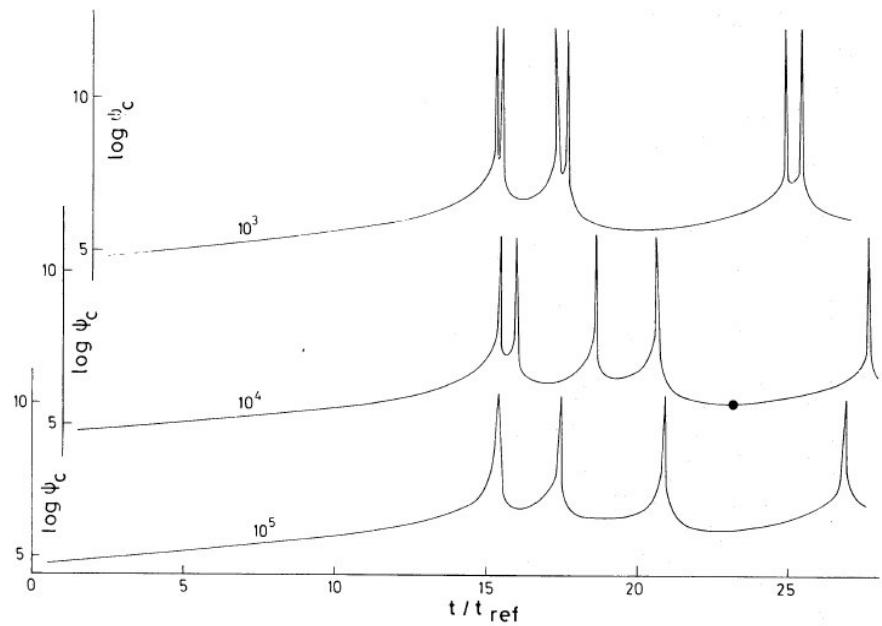
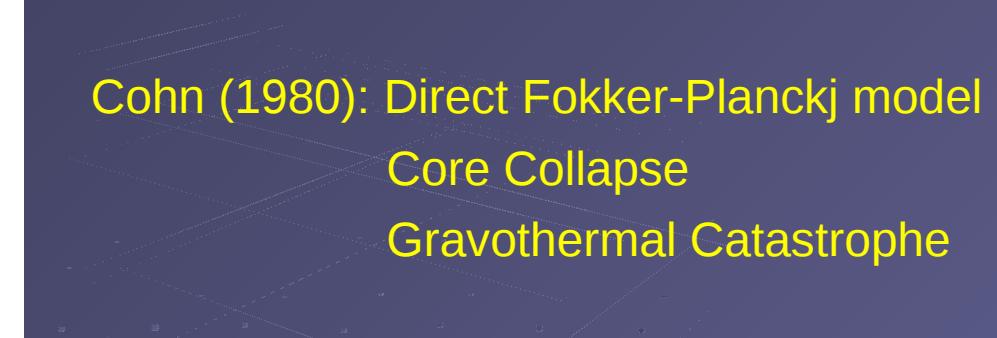


Hubble Space Telescope • WFPC2

# Theoretical Modelling: Gas Sphere Gravothermal Expansion!

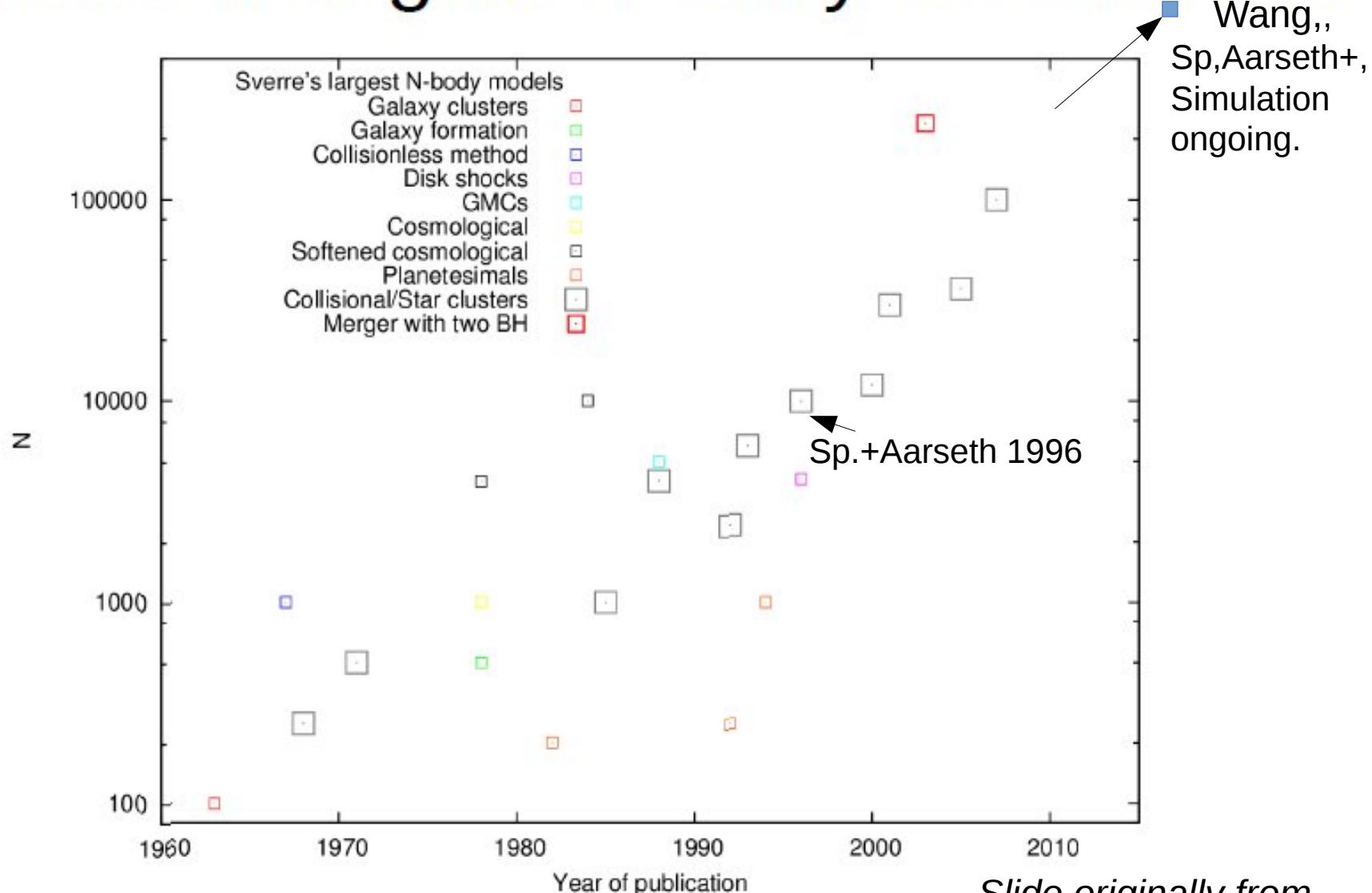


Bettwieser & Sugimoto 1984:  
Gravothermal Oscillations by  
energy generation from binaries  
(cf. nuclear stellar energy generation)



**Figure 1.** The ‘central’ density  $\psi_c$  is plotted against the non-dimensional time  $t/t_{\text{ref}}$  for  $k = 2$  models with three different values of  $C$  as attached to each curve. Note, that if they were plotted with the same ordinate they would be close to each other despite the great differences in  $C$ . The model indicated with a filled circle will be compared with King’s model in Section 4.2.

# Sverre's largest N-body simulations

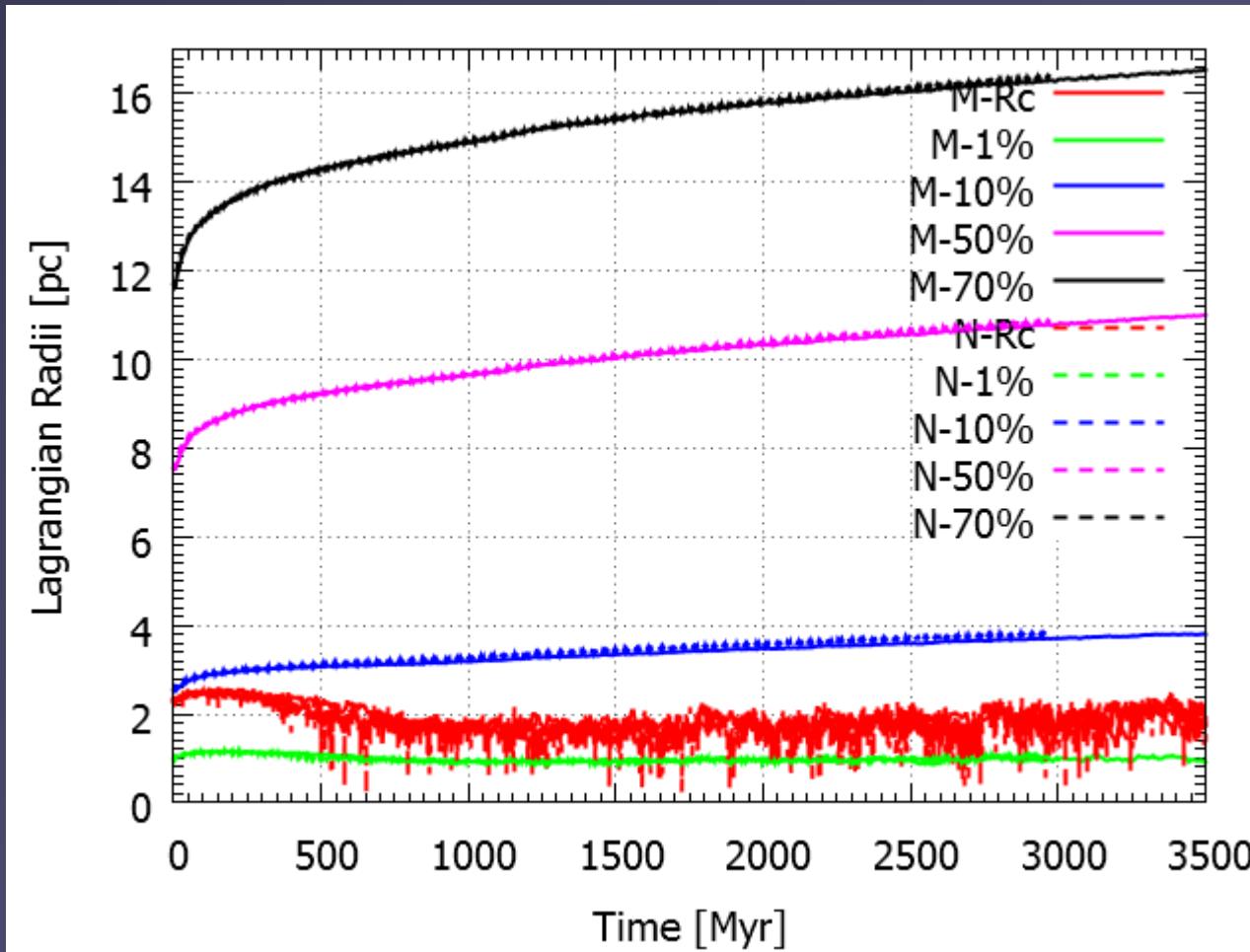


Criteria: published results, evolution well advanced

Slide originally from  
Douglas C. Heggie,  
citations added by RS

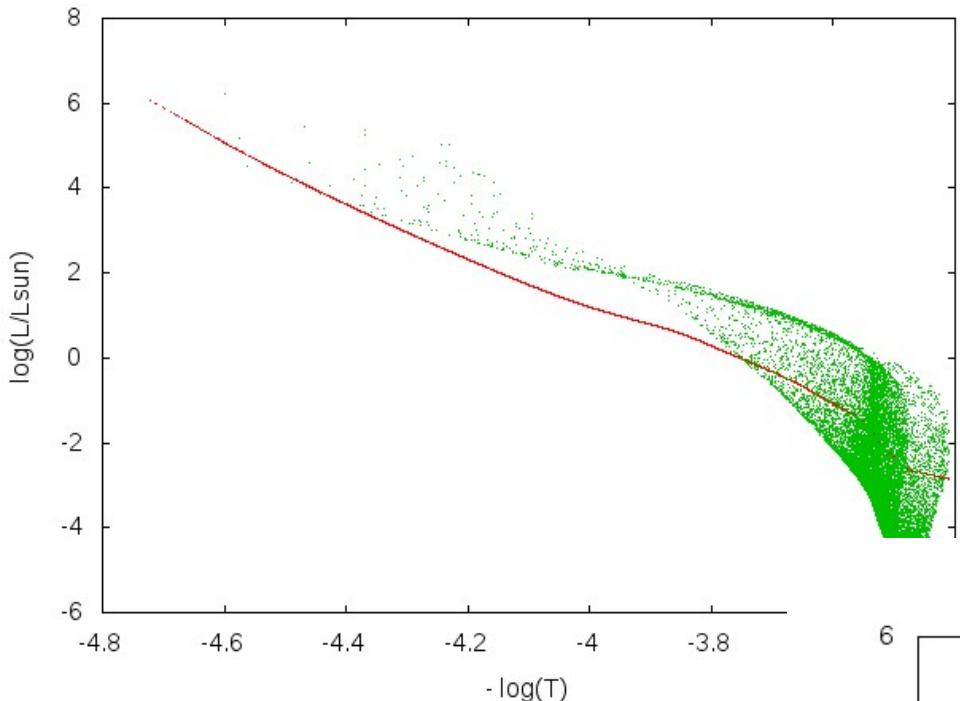
# Direct Simulation (Poster Long Wang)

## NBODY6++GPU 1 Million Bodies



Wang, Spurzem, Aarseth, Berczik, Nitadori, Kouwenhoven, Naab 2015a subm. MNRAS,  
Used RZG Garching hydra Wang et al. 2015b, in prep.  
GPU cluster (400 Kepler GPUs) Aspen Jan. 2015

$t=0$



Preliminary Results

$N=256k$  star cluster

10% initial binaries

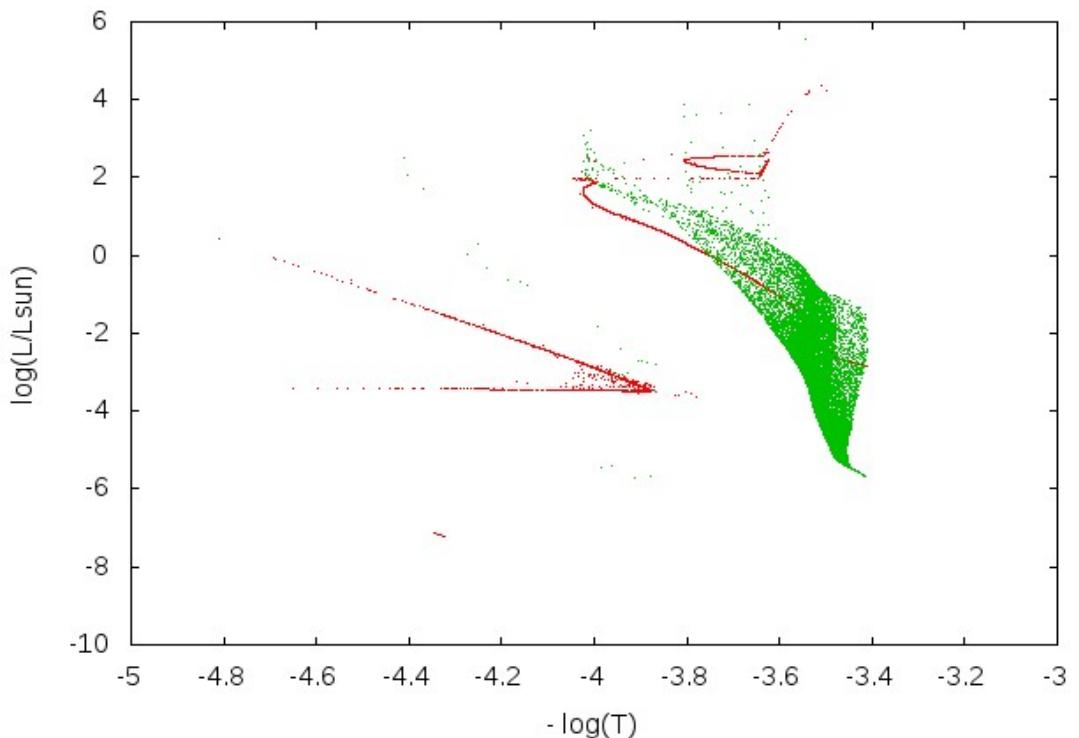
Wang, Spurzem, Aarseth, Berczik, +

Left: initial HR diagram

Right: after 2 Gyrs

...ongoing 1M ...

$t=2 \text{ Gyr}$



Sorry!

Problem with Plot of  
Binaries.

.. work ongoing ...

Long Wang et al.

# Theoretical Modelling: Moment Models

16 Schneider, Amaro-Seoane & Spurzem 2011

	$a_p$ [ $\frac{\text{km}^2}{\text{s}^2 \text{pc}^3}$ ]	$F$ [ $\frac{\text{km}^3}{\text{s}^3 \text{pc}^3}$ ]	$a_F$ [ $\frac{\text{km}^3}{\text{s}^3 \text{pc}^3}$ ]	$\kappa$ [ $\frac{\text{km}^4}{\text{s}^4 \text{pc}^3}$ ]	$a_{\kappa 1}$ [ $\frac{\text{km}^4}{\text{s}^4 \text{pc}^3}$ ]	$a_{\kappa 2}$ [ $\frac{\text{km}^4}{\text{s}^4 \text{pc}^3}$ ]	$G$ [ $\frac{\text{km}^5}{\text{s}^5 \text{pc}^3}$ ]	$a_{G1}$ [ $\frac{\text{km}^5}{\text{s}^5 \text{pc}^3}$ ]	$a_{G2}$ [ $\frac{\text{km}^5}{\text{s}^5 \text{pc}^3}$ ]
FIG. 2.	<i>left</i>	0	0	0	0	0	0	0	0
	<i>right</i>	0	0	0	$1.5 \cdot 10^5$	0	0	0	0
FIG. 3.	<i>left</i>	-5	0	0	$1.5 \cdot 10^5$	0	0	0	0
	<i>right</i>	3.3	0	0	$1.5 \cdot 10^5$	0	0	0	0
FIG. 4.	<i>left</i>	0	$-2.5 \cdot 10^2$	0	$1.5 \cdot 10^5$	0	0	0	0
	<i>right</i>	0	$3.5 \cdot 10^2$	0	$1.5 \cdot 10^5$	0	0	0	0

$$F = -2.5 \cdot 10^2 \text{ km}^3 \text{s}^{-3} \text{pc}^{-3}$$

$$F = 3.5 \cdot 10^2 \text{ km}^3 \text{s}^{-3} \text{pc}^{-3}$$

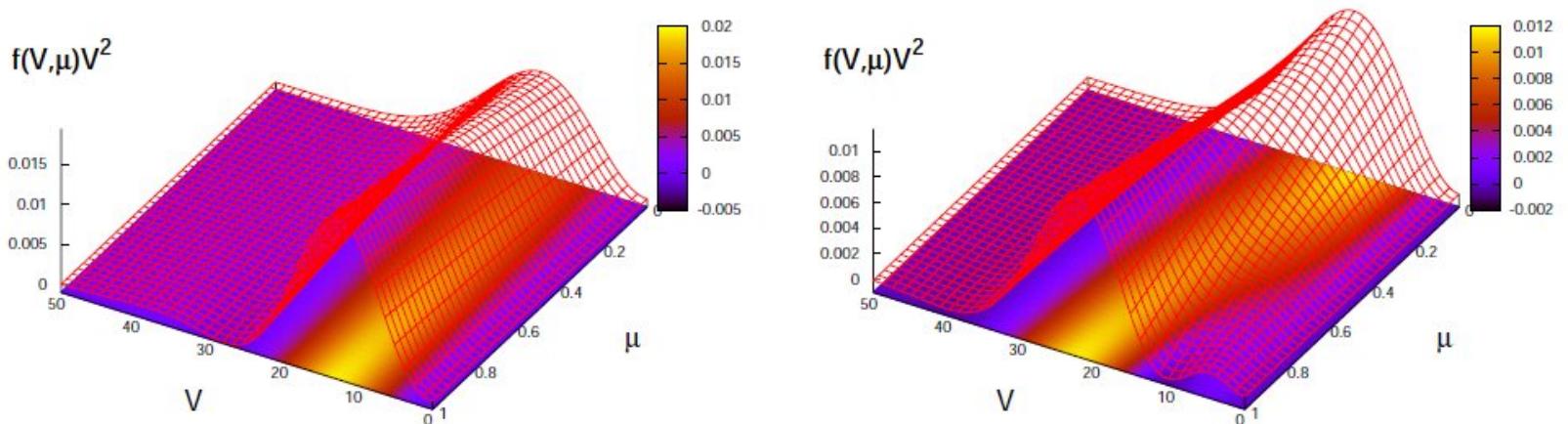


Figure 4. VDF with two different values for the third order total moment  $F$  corresponding to energy flux. *left:* Shows the effect of negative  $F$  on a MB distribution. *right:* The effect of positive  $F$  on a MB distribution

# Compact Binaries in Star Clusters I - Black Hole Binaries Inside Globular Clusters

MNRAS 2010

J. M. B. Downing<sup>3\*</sup>, M. Benacquista<sup>4</sup>, R. Spurzem<sup>1,2,3</sup>, and M. Giersz<sup>5</sup>

<sup>1</sup>*National Astronomical Observatories, Chinese Academy of Sciences, 20A Datun Ln, Chaoyang District, 100012, China*

<sup>2</sup>*Kavli Institute of Astronomy and Astrophysics, Peking University, Beijing, China*

<sup>3</sup>*Astronomisches Rechen-Institut, Zentrum für Astronomie der Universität Heidelberg, Monchhofsstraße 12-14, D-69120 Heidelberg, Germany*

<sup>4</sup>*Center for Gravitational Wave Astronomy, University of Texas at Brownsville, Brownsville, TX 78520, USA*

<sup>5</sup>*Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, ul. Bartycka 18, 00-716 Warsaw, Poland*

# Compact Binaries in Star Clusters II - Escapers and Detection Rates

MNRAS 2011

J. M. B. Downing<sup>1,2\*</sup>, M. J. Benacquista<sup>3</sup>, M. Giersz<sup>4</sup>, and R. Spurzem<sup>5,6,1</sup>

<sup>1</sup>*Astronomisches Rechen-Institut, Zentrum für Astronomie der Universität Heidelberg, Monchhofsstraße 12-14, D-69120 Heidelberg, Germany*

<sup>2</sup>*Fellow of the International Max-Planck Research School for Astronomy and Cosmic Physics at the University of Heidelberg, Heidelberg, Germany*

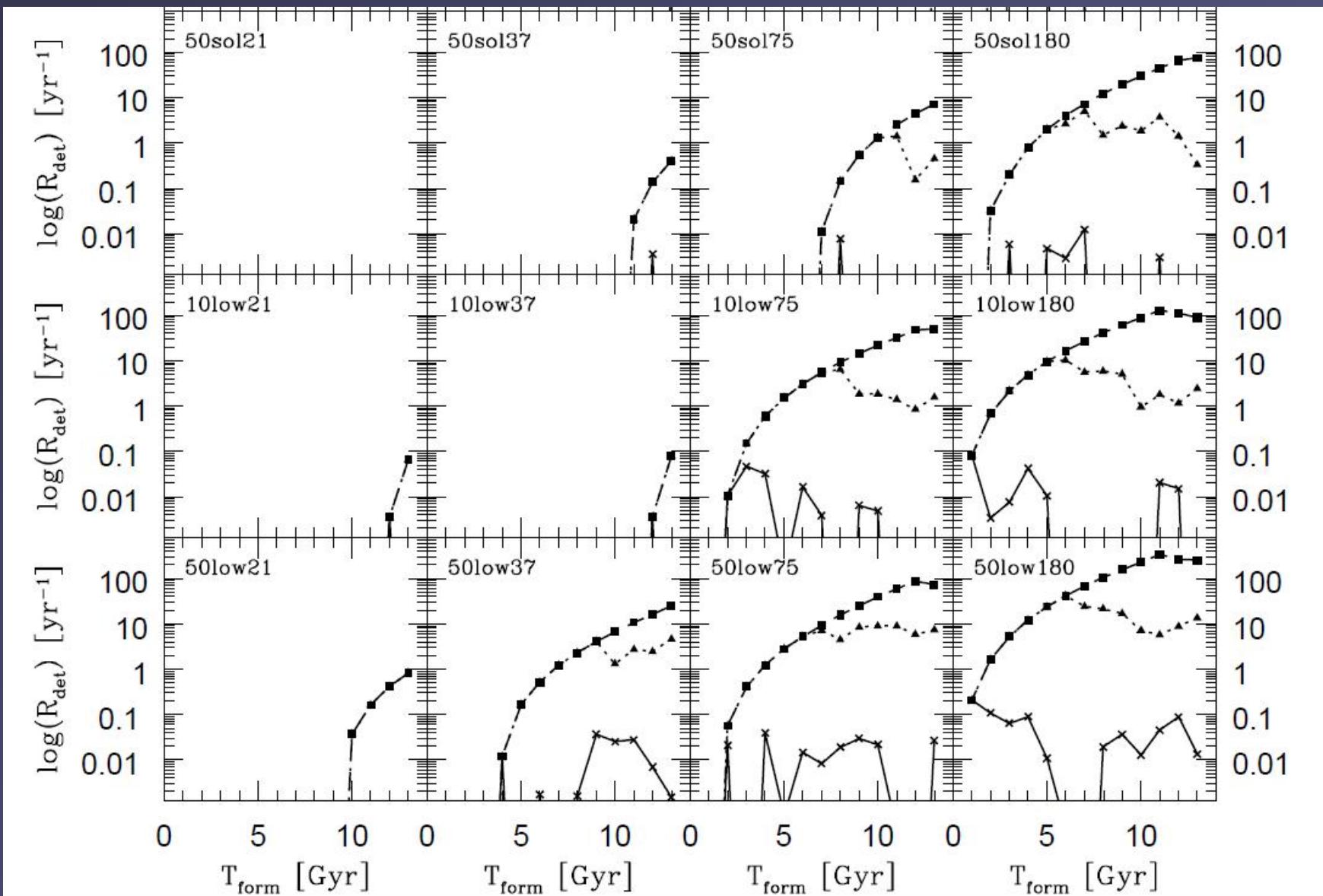
<sup>3</sup>*Center for Gravitational Wave Astronomy, University of Texas at Brownsville, Brownsville, TX 78520, USA*

<sup>4</sup>*Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, ul. Bartycka 18, 00-716 Warsaw, Poland*

<sup>5</sup>*National Astronomical Observatories, Chinese Academy of Sciences, 20A Datun Rd., Chaoyang District, 100012, China*

<sup>6</sup>*Kavli Institute of Astronomy and Astrophysics, Peking University, Beijing, China*

# Downing et al. 2011



# Theoretical Models II: Fokker-Planck

$$\frac{\partial f}{\partial t} + \frac{\partial \phi}{\partial t} \frac{\partial f}{\partial E} = \left( \frac{\partial f}{\partial t} \right)_{\text{enc}},$$

with the potential  $\phi$  advanced according to the Poisson equation

$$\nabla^2 \phi = 4\pi G n,$$

and the collisional term on the right-hand side of equation (1) expressed under the Fokker-Planck assumption of small scatterings:

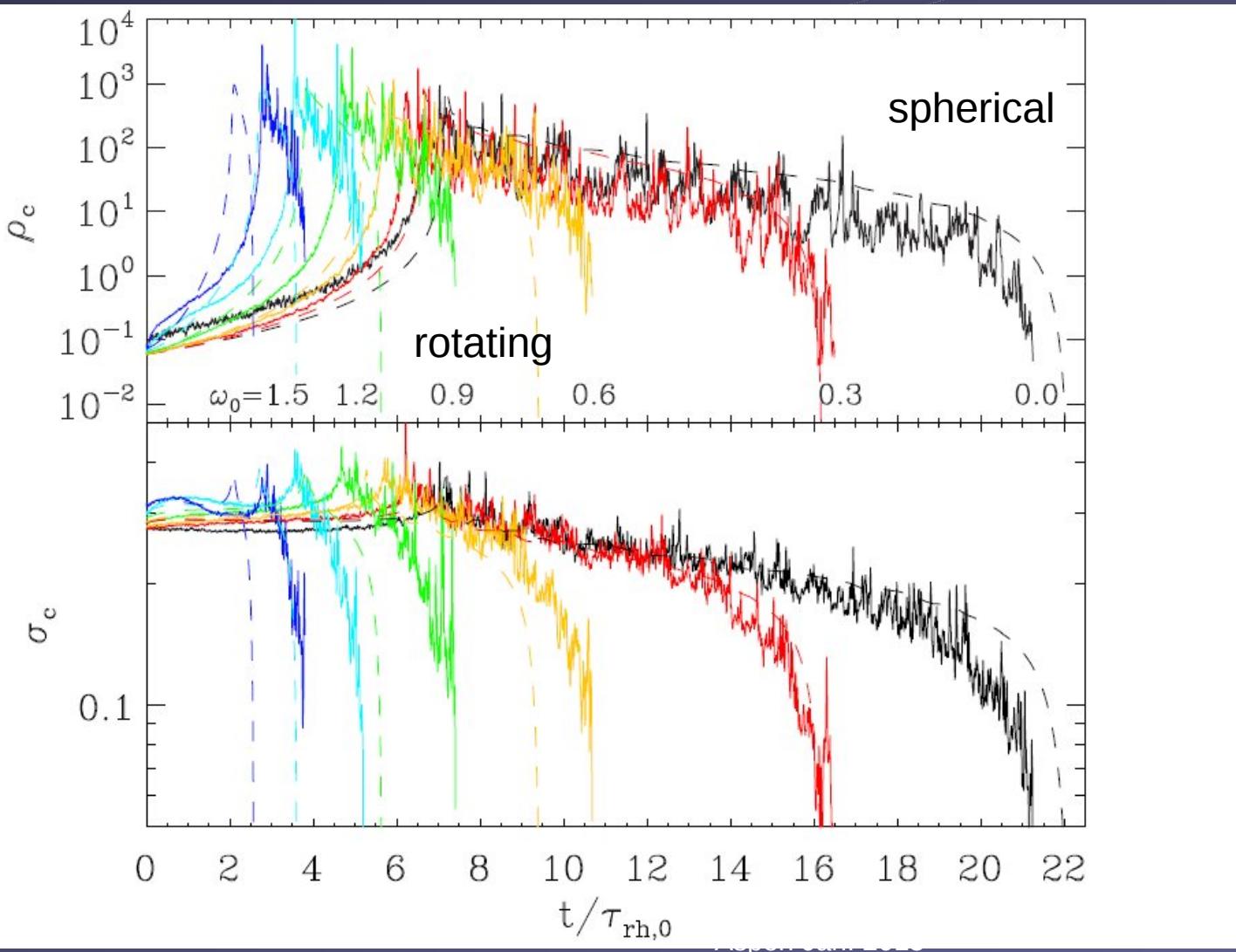
$$\begin{aligned} \left( \frac{\partial f}{\partial t} \right)_{\text{enc}} = & \frac{1}{V} \left[ -\frac{\partial}{\partial E} (\langle \Delta E \rangle f V) - \frac{\partial}{\partial J_z} (\langle \Delta J_z \rangle f V) \right. \\ & + \frac{1}{2} \frac{\partial^2}{\partial E^2} (\langle (\Delta E)^2 \rangle f V) + \frac{\partial^2}{\partial E \partial J_z} (\langle \Delta E \Delta J_z \rangle f V) \\ & \left. + \frac{1}{2} \frac{\partial^2}{\partial J_z^2} (\langle (\Delta J_z)^2 \rangle f V) \right], \end{aligned}$$

Orbit averaged  
Fokker-Planck  
Equation

(here in the 2D  
form for axisymm.  
systems,  
Einsel & Spurzem  
1999)

# Theoretical Models II: Fokker-Planck

## Dissolution of Star Cluster in Tidal Field



Kim, Yoon,  
Lee, Spurzem,  
2008, MNRAS

Hong, Kim,  
Lee, Spurzem,  
2013, MNRAS

Three Phases in  
Cluster Dissolution:

- 1) Core Collapse  
(Encounters)
- 2) Post-Collapse  
Steady Evaporation  
(Encount)
- 3) Dynamic  
final dissolution

# Star Cluster Simulations – Key Issues

- Theoretical Models / Large N-Body Models
- Black Holes and Tidal Disruption/Star Accretion
- Accelerated Computing (GPU)

Aspen Jan. 2015



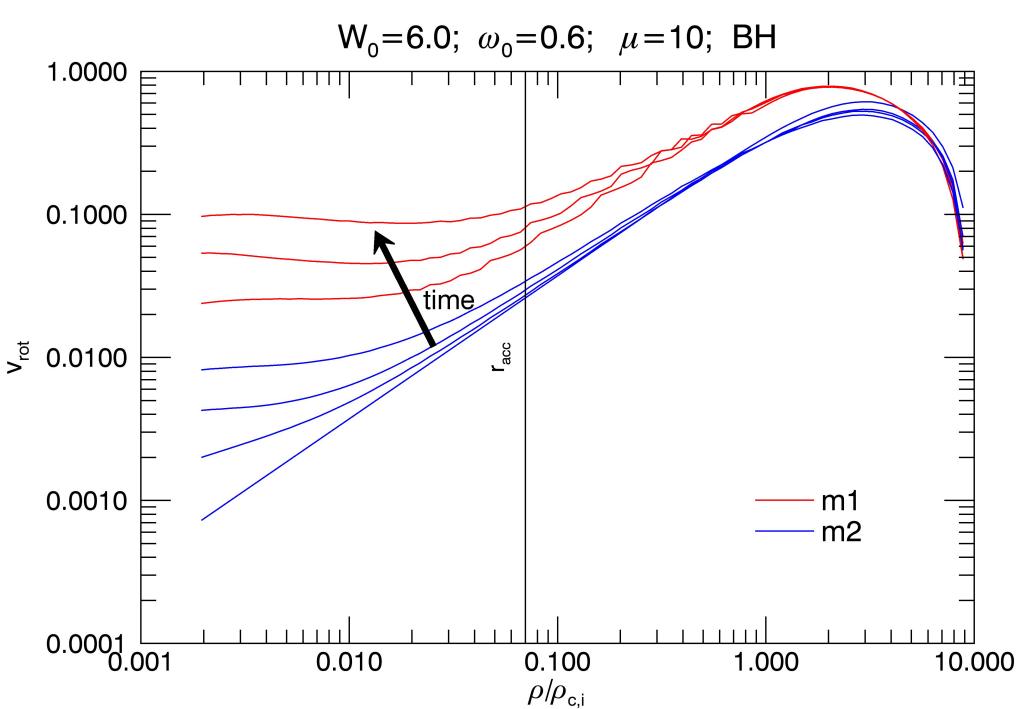
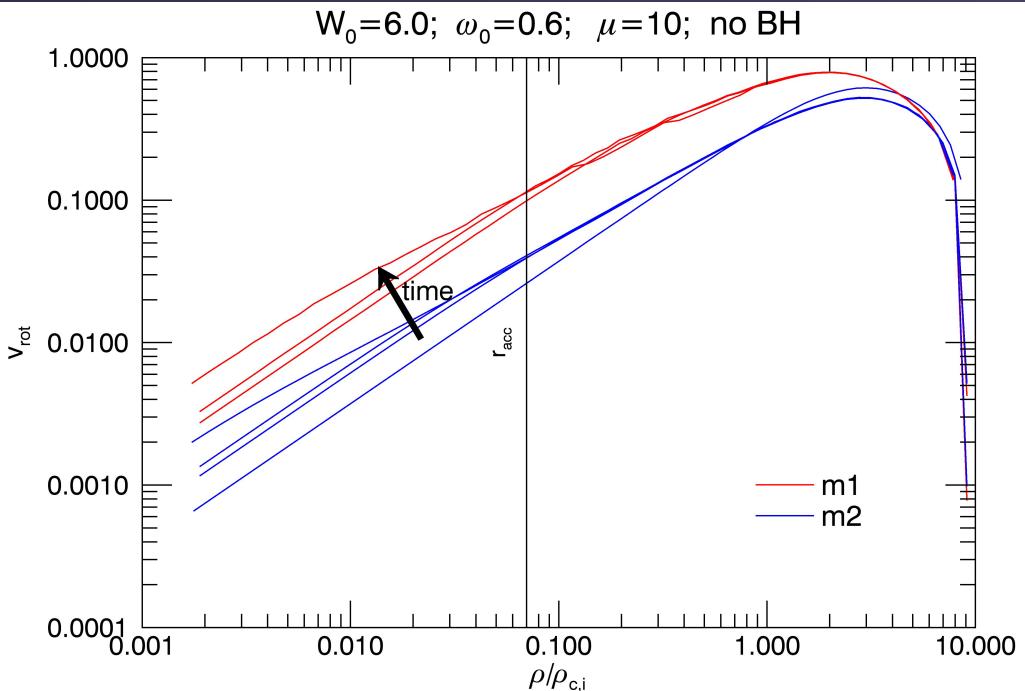
Hubble Space Telescope • WFPC2

# Theoretical Models II: Fokker-Planck

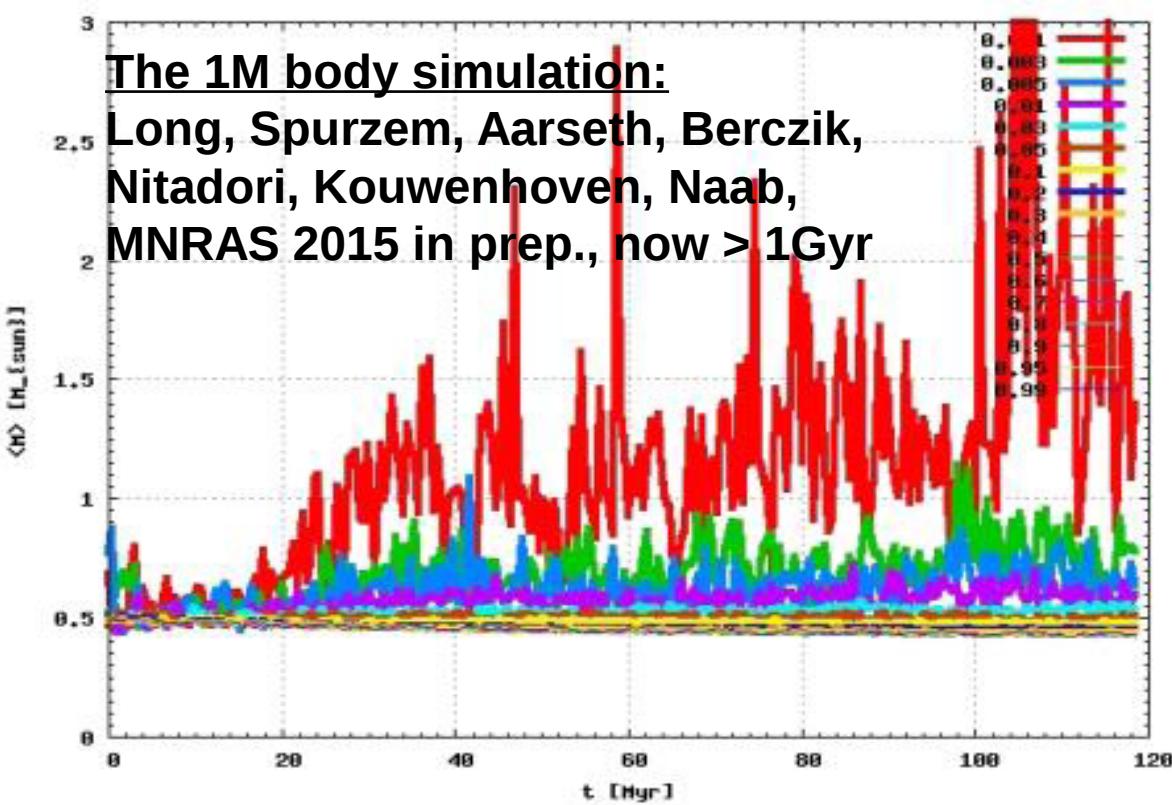
Fiestas, Preto, Berczik,  
Spurzem, Lee, 2015 in prep.

**Two Masses, Rotation,  
with and without black hole**

**N-Body?**



# Intermediate Mass Black Hole?

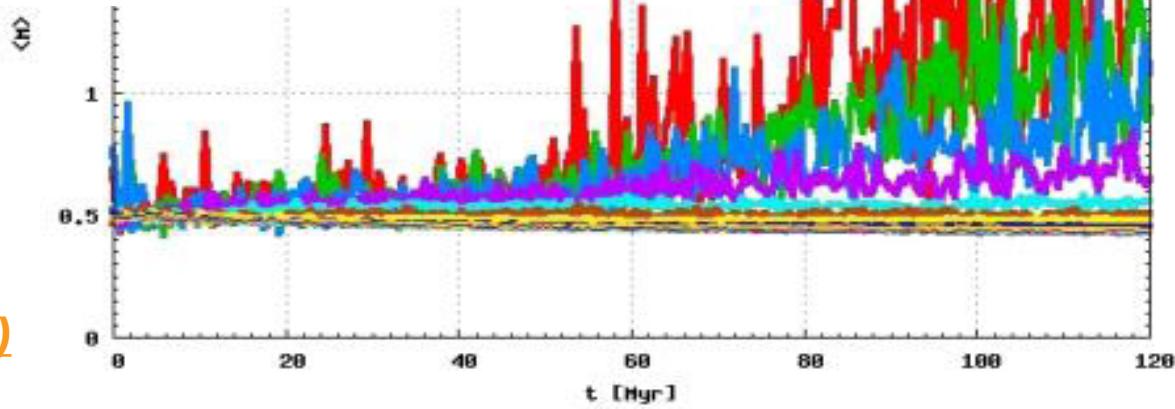


With IMBH →  
Slow mass segregation

Used RZG Garching hydra  
GPU cluster (400 Kepler GPUs)

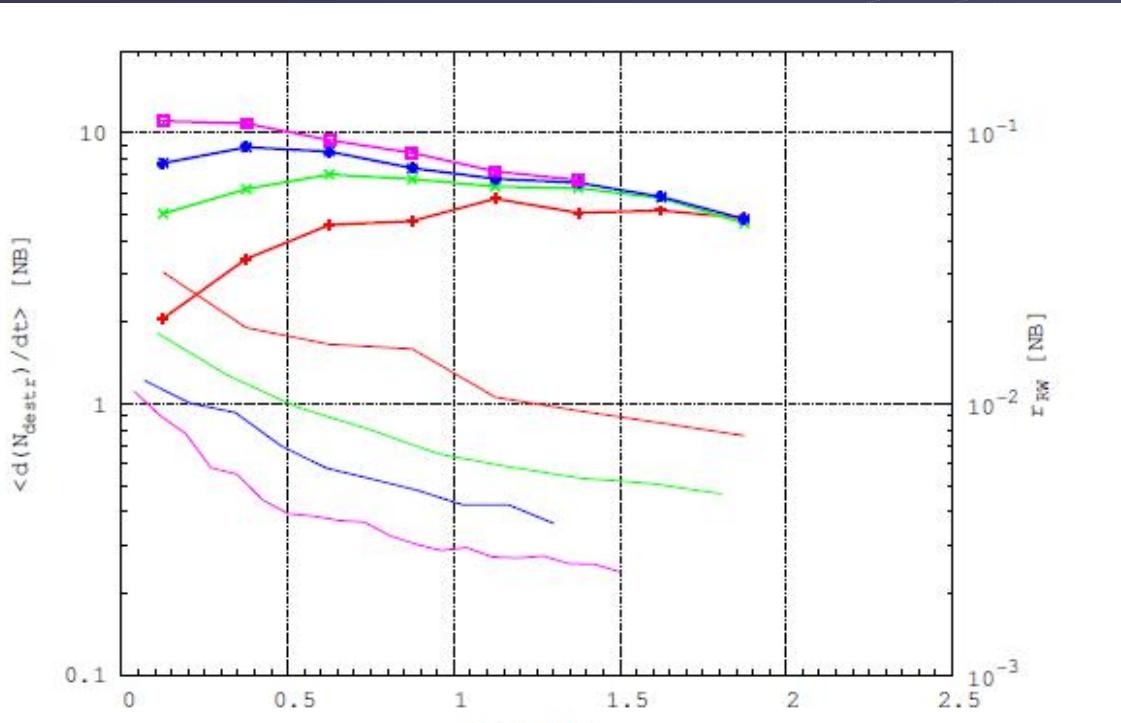
← without IMBH  
Fast mass segregation

Red line: average  
Stellar mass  
In inner shell



# Tidal Disruption of Stars in Nuclear Star Clusters around SMBH

## Paper I: Spherical Models



Standard 2-b relax. / empty loss cone (Frank/Rees 76)  
works extremely well, in spherical systems...

FIG. 2.—  $x$  axis is time expressed in unit of initial half-mass relaxation time( $t_{rh}$ ), left  $y$  axis is the averaged disruption rate in a given time range( i.e.  $1/4 t_{rh}$ ). The unit for disruption rate is number of disrupted stars per unit time. Right  $y$  axis is the Brownian motion amplitude. Curves with symbols are TD rate for  $r_t = 10^{-3}$ , from bottom to top, respond for  $N=16k, 32k, 64k$  and  $128k$ . Curves without symbols shows black hole's Brownian motion amplitude for  $N=16k, 32k, 64k$  and  $128k$ (from top to bottom)

Large N-Body Simulations  
phiGPU  
(Zhong, Berczik,  
Spurzem 2014, ApJ)

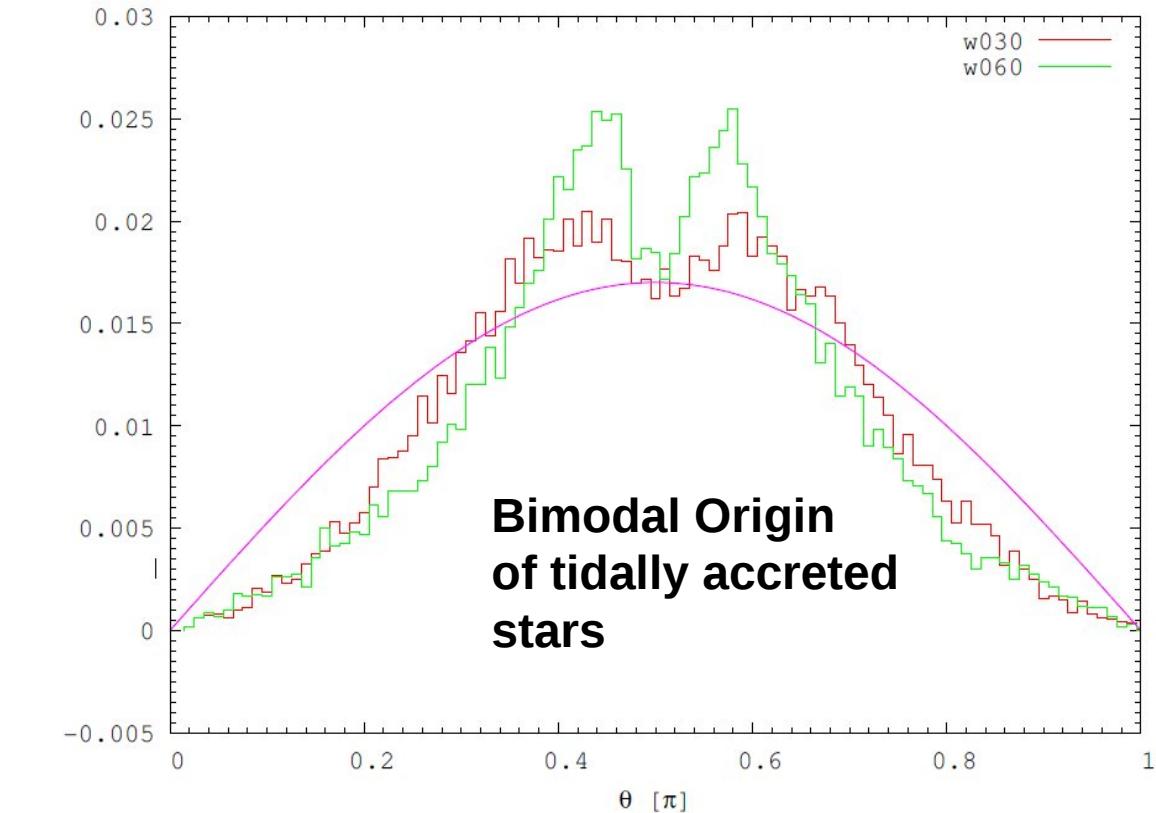
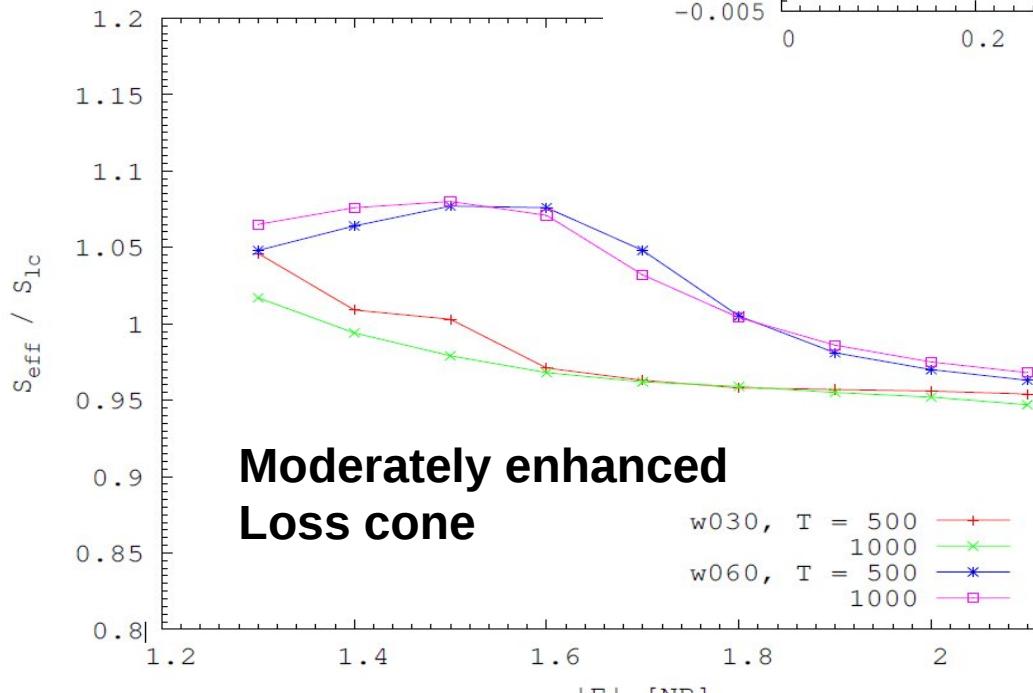
Using  
NAOC GPU Cluster

(See also  
Li, Liu, Berczik, Chen,  
Spurzem, 2012)

# Tidal Disruption of Stars in Nuclear Star Clusters around SMBH

## Paper II: Rotating Axisymmetric Models

Zhong, Berczik,  
Spurzem, to be subm.  
MNRAS Feb 2015



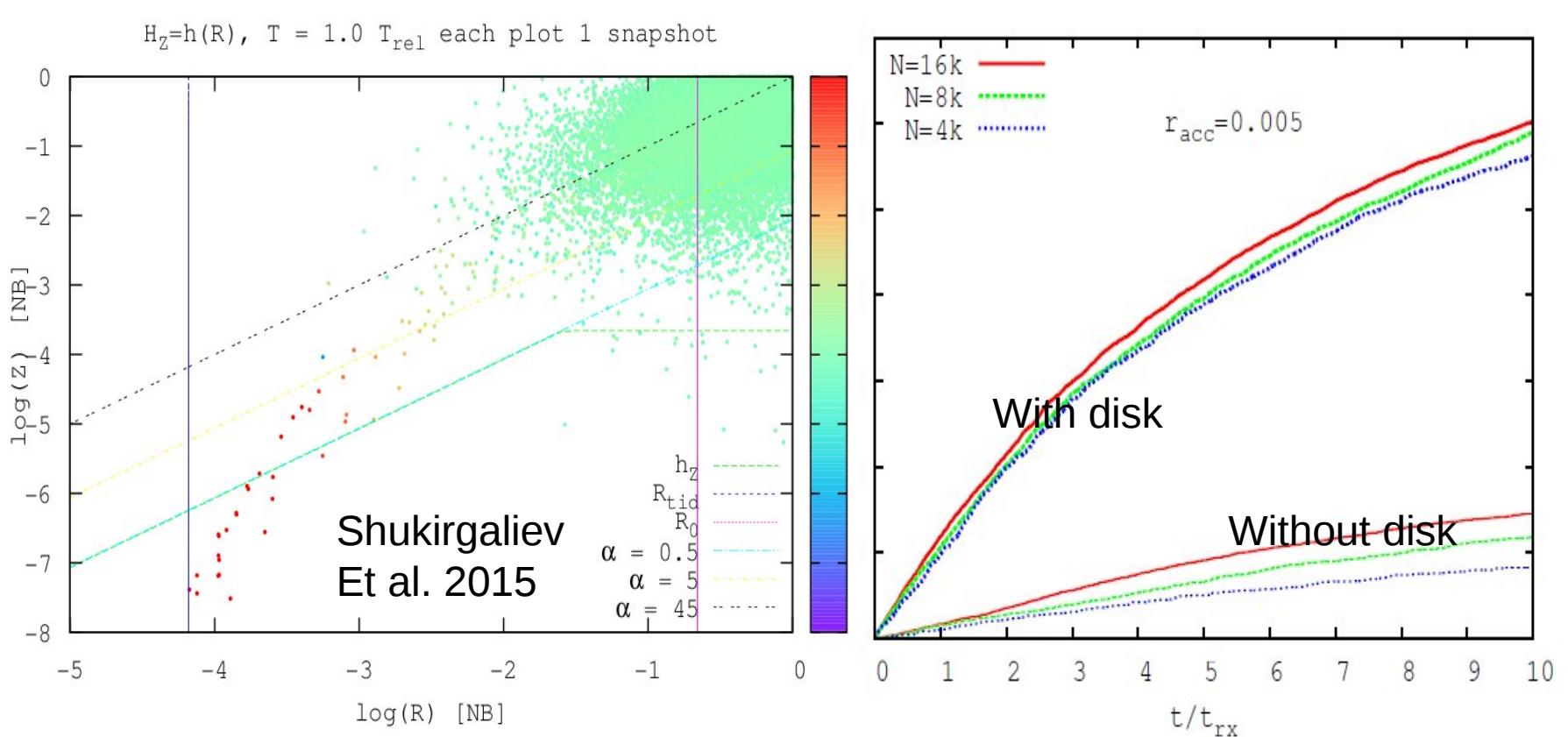
# Star-Disk Interactions enhance tidal accretion rate in star clusters with BH

Just, ... Berczik, Spurzem, ..., 2012, ApJ (Paper I)

Kennedy et al. 2015 in prep. (Paper II)

Shukirgaliev et al. 2015 in prep. (Paper III)

The presence of an accretion disk near an SMBH enhances the mass growth rate of SMBH by factor 3 and creates a stellar disk.



# Star Cluster Simulations – Key Issues

- Theoretical Models / Large N-Body Models
- Black Holes and Tidal Disruption/Star Accretion
- Accelerated Computing (GPU)

Aspen Jan. 2015



Rank	Site	Top 10 List June 2012 System		Cores	Rmax (TFlop/s)	Rpeak (TFlop/s)	Power (kW)
1	National University of Defense Technology China	Tianhe-2 (MilkyWay-2) - TH-IVB-FEP Cluster, Intel Xeon E5-2692 12C 2.200GHz, TH Express-2, Intel Xeon Phi 31S1P NUDT		3120000	33862.7	54902.4	17808
2	DOE/SC/Oak Ridge National Laboratory United States	Titan - Cray XK7 , Opteron 6274 16C 2.200GHz, Cray Gemini interconnect, NVIDIA K20x Cray Inc.		560640	17590.0	27112.5	8209
3	DOE/NNSA/LLNL United States	Sequoia - BlueGene/Q, Power BQC 16C 1.60 GHz, Custom IBM		1572864	17173.2	20132.7	7890
4	RIKEN Advanced Institute for Computational Science (AICS) Japan	K computer, SPARC64 Vlllfx 2.0GHz, Tofu interconnect Fujitsu		705024	10510.0	11280.4	12660
5	DOE/SC/Argonne National Laboratory United States	Mira - BlueGene/Q, Power BQC 16C 1.60GHz, Custom IBM		786432	8586.6	10066.3	3945
6	Texas Advanced Computing Center/Univ. of Texas United States	Stampede - PowerEdge C8220, Xeon E5-2680 8C 2.700GHz, Infiniband FDR, Intel Xeon Phi SE10P Dell		462462	5168.1	8520.1	4510
7	Forschungszentrum Juelich (FZJ) Germany	JUQUEEN - BlueGene/Q, Power BQC 16C 1.600GHz, Custom Interconnect IBM		458752	5008.9	5872.0	2301
8	DOE/NNSA/LLNL United States	Vulcan - BlueGene/Q, Power BQC 16C 1.600GHz, Custom Interconnect IBM		393216	4293.3	5033.2	1972
9	Leibniz Rechenzentrum Germany	SuperMUC - iDataPlex DX360M4, Xeon E5-2680 8C 2.70GHz, Infiniband FDR		147456	2897.0	3185.1	3423

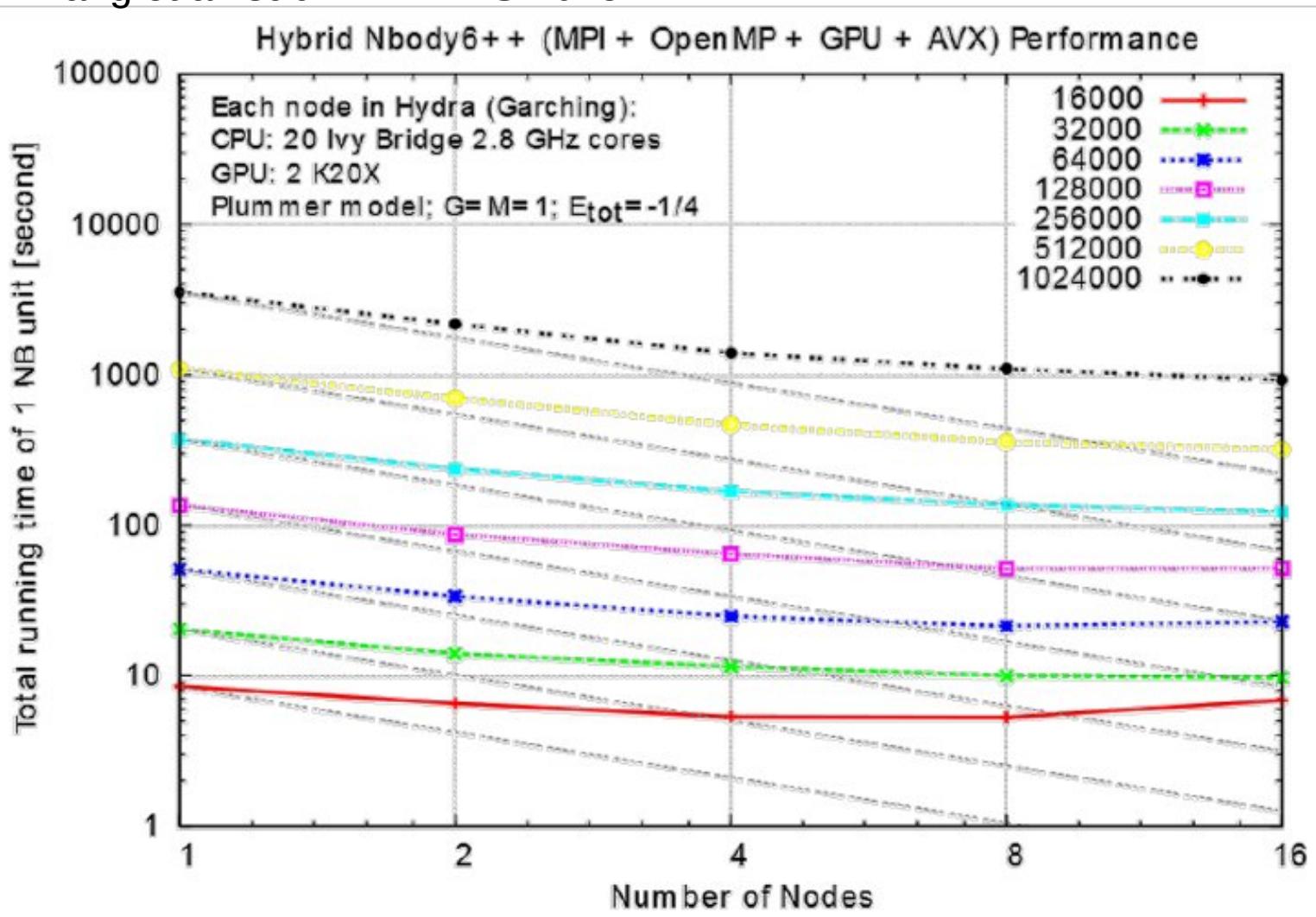
# NAOC laohu cluster



# NBODY6++GPU (Poster Long Wang)

## PERFORMANCE OF HYBRID MPI

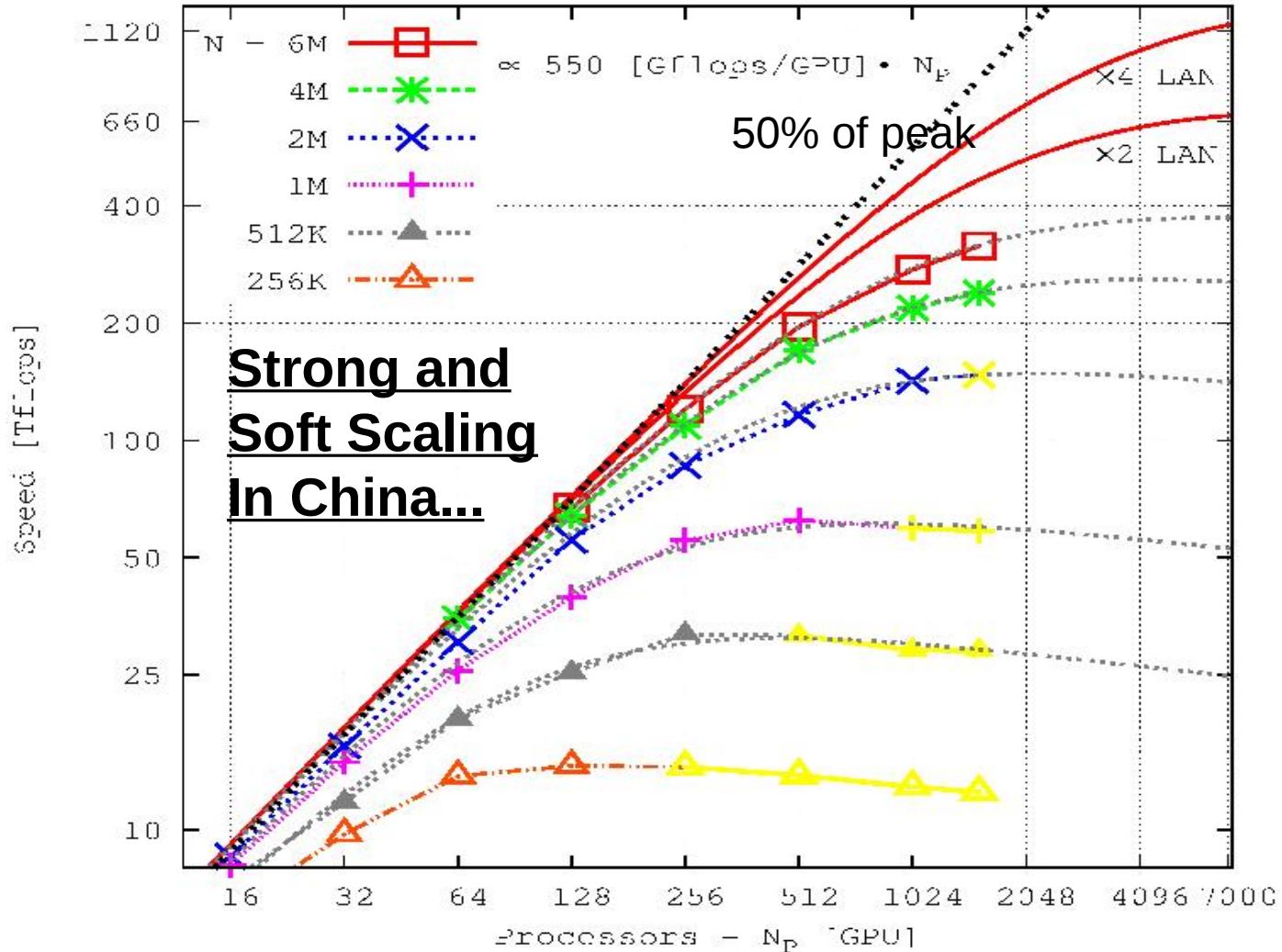
Wang et al. subm. MNRAS 2015



350 Teraflop/s  
1600 GPUs.  
440 cores  
 $= 704.000$   
GPU-Cores

Using  
Mole-8.5  
of  
IPE/CAS  
Beijing

Spurzem et al.,  
2013, Lect.  
Notes Comp.  
Phys., Springer



# Summary/Future

## Astrophysical High Precision N-Body -

- Data Mining for million body simulations
- Rotation compare with theory
- Binaries, Collision Products
- Tidal Star Accretion with Black Hole

## Some More Astrophysical Science Drivers:

GW Sources in Star Clusters / Gal. Nuclei

No Evidence of Stalling of Binary Black Holes -  
Coalescence in 0.1 – 1.0 Gyrs in full simulation



中国科学院国家天文台

NATIONAL ASTRONOMICAL OBSERVATORIES, CHINESE ACADEMY OF SCIENCES



北京大学  
PEKING UNIVERSITY